$Summary\ of\ ``Quantum-limit\ Chern\ Topological\ Magnetism\ in\ TbMn_6Sn_6"$

Kevin Y. Lin

Freshman, Southern University of Science and Technology (SUSTech) Shenzhen, Guangdong, China

(7/8/2025)

Background

In Kagome materials with strong spin-orbit coupling and out-of-plane magnetization, spin-polarized Dirac fermions are theoretically possible, analogous to the Haldane model. However, ideal quantum materials are lacking, posing experimental challenges.

Key Findings / Evidence of Quantum-limit Chern Magnet

Spin-polarized Dirac cones with Landau Quantization

(1) Zero-field STM peak moves linearly with magnetic field (Zeeman effect):

$$\Delta E = \pm \frac{1}{2} g \mu_B B.$$

Indicates spin-polarized electronic states.

- (2) STM dI/dV maps at high magnetic field show discrete Landau quantization, observing clear Dirac dispersion and characteristic E_n vs. B dependence.
- (3) ARPES measurements confirm Dirac fermions in the Brillouin Zone.

Chern Gap

- (1) Landau fan: High-bias STM measurements under varying magnetic fields show two parallel straight lines, revealing a Chern gap.
- (2) Landau-level fitting formula:

$$E_n(B) = \pm \sqrt{\left(\frac{\Delta}{2}\right)^2 + 2e\hbar v_F^2 |n|B} - \frac{1}{2}g\mu_B B,$$

with fitted parameters:

$$\Delta = 34 \pm 2 \, \mathrm{meV}, \quad E_D = 130 \, \mathrm{meV}, \quad v_F = 4.2 \times 10^5 \, \mathrm{m/s}.$$

Bulk-boundary Correspondence and Dissipationless Edge States

- STM dI/dV mapping (Fig. 4a) clearly demonstrates localized in-gap edge states at step edges (interfaces between Kagome lattice layers).
- Edge states appear due to topological properties, as the bulk is insulating:

$$n_{\text{edge}} = C \, (\text{Chern number})$$

• Authors conducted an experiment, revealing dissipationless edge states by low QPI peaks (Fourier transforms) in Fig. 4b.

Quantum Limit

- (1) Low carrier concentration: The Fermi level is very close to the Dirac point, leading to extremely low carrier density and symmetric electron-hole excitations [?].
- (2) Discrete and sparse Landau levels (Fig. 2b).

Anomalous Hall Effect (AHE)

• AHE arises due to intrinsic Berry curvature:

$$\rho_{xy}^{AHE} = \alpha \rho_{xx} + \beta \rho_{xx}^2 + \gamma \rho_{xy}^2.$$

- Experimentally observed strong linear relationship between ρ_{xy}^{AHE} and ρ_{xx}^2 , confirming intrinsic Berry curvature dominance.
- Verification of Chern gap via Berry curvature:

$$\sigma_{xy} = -\frac{e^2}{h} \frac{1}{N} \sum_n \int_{BZ} \frac{d^2k}{(2\pi)^2} f_n(\mathbf{k}) \Omega_n(\mathbf{k}),$$

Substituting $\Delta \approx 34\,\mathrm{meV}$ and $E_D \approx 130\,\mathrm{meV}$ gives theoretical $\sigma_{xy}^{\mathrm{Berry}} = 0.13\,e^2/h$, matching experimentally measured $0.14\,e^2/h$, confirming Berry curvature origin.

Research Significance

- First experimental evidence of a "quantum-limited Chern topological magnet" [?].
- Establishes an experimental framework demonstrating bulk-boundary-Berry correspondence in topological magnets.

References

- Physical Review X 14, 011047 (2024). https://doi.org/10.1103/PhysRevX.14.011047
- Yin, J.-X., Ma, W., Cochran, T. A., et al. (2020). Quantum-limit Chern topological magnetism in TbMn₆Sn₆. *Nature*, 583, 533–536.https://doi.org/10.1038/s41586-020-2482-7